

AT (A)

$$i_1 + i_2 = i_3$$

AT (B)

$$0 = i_2 + i_4 + i_5$$

AT (C)

$$i_2 + i_4 + i_5 = i_6$$

AT (D)

$$i_3 + i_6 = i_1$$

$$i_6 = -i_2$$

Left Loop start D clockwise

$$-i_1 5\Omega + 10V - i_1 6\Omega - i_3 7\Omega = 0$$

$$+ 20V + i_4 (1\Omega) + 5V - i_2 (4\Omega)$$

$$- i_3 (7\Omega) = 0$$

$$+ i_5 (8\Omega) + 15V + i_5 (2\Omega) + i_5 (3\Omega) - i_4 (1\Omega)$$

$$- 20V = 0$$

$$\hat{i}_1 = -0.3211 \text{ A}$$

$$\hat{i}_2 = +2.2543 \text{ A}$$

$$\hat{i}_3 = 1.9332 \text{ A}$$

$$\hat{i}_4 = -2.4504 \text{ A}$$

$$\hat{i}_5 = 0.1961 \text{ A}$$

$$\Delta V_{A \rightarrow D} = -\hat{i}_3 7\Omega = -(1.9332 \text{ A})(7\Omega)$$

$$\Delta V_{A \rightarrow D} = \underline{-13.5 \text{ V}}$$

$$\Delta V_{A \rightarrow D} = +\hat{i}_1 6\Omega - 10\text{V} + \hat{i}_1 5\Omega$$

$$\Delta V_{A \rightarrow D} = +\hat{i}_1 (6\Omega + 5\Omega) - 10\text{V}$$

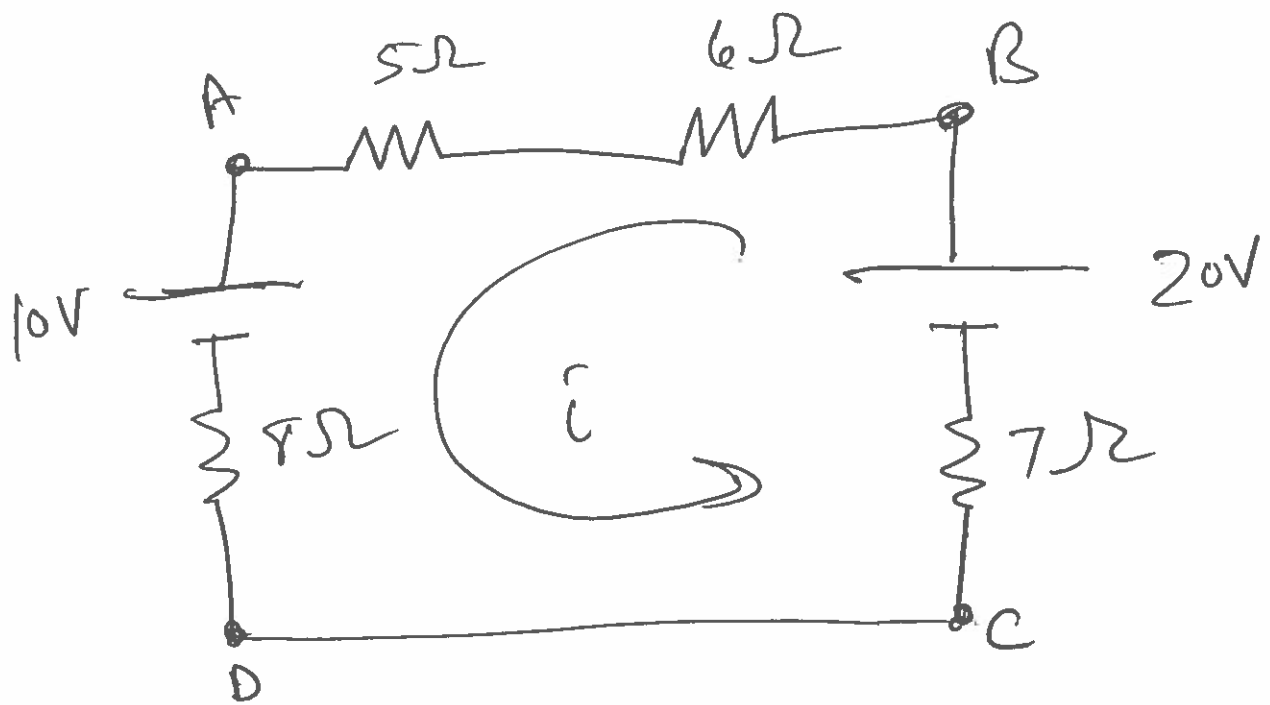
$$= +(-0.3211 \text{ A})(11\Omega) - 10\text{V}$$

$$= \underline{-13.5 \text{ V}}$$

$$\Delta V_{C \rightarrow B} = +20\text{V} + \hat{i}_4 (1\Omega)$$

$$= 20\text{V} + (-2.4504 \text{ A})(1\Omega)$$

$$= \textcircled{+17.55 \text{ V}}$$



$$\Delta V_{A \rightarrow B} = ? = +i(5\Omega + 6\Omega)$$

$$i = \frac{V_{TOT}}{R_{TOT}} = \frac{20V - 10V}{5\Omega + 6\Omega + 7\Omega + 8\Omega} = \frac{10V}{26\Omega}$$

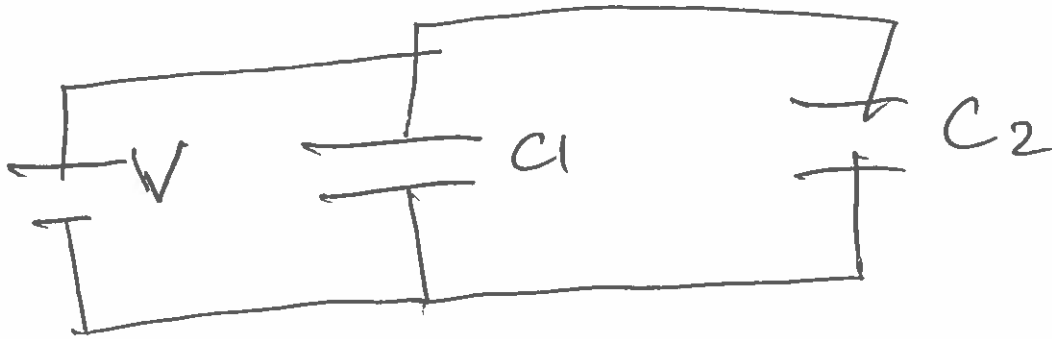
$$i = 0.385A$$

$$\Delta V_{A \rightarrow B} = (0.385A)(11\Omega)$$

$$= +4.235V$$

$$\boxed{+4.235V}$$

# Capacitors in Series / Parallel



$$Q_1 = C_1 V \quad Q_2 = C_2 V$$

$$Q_{\text{Tot}} = Q_1 + Q_2 = C_1 V + C_2 V$$

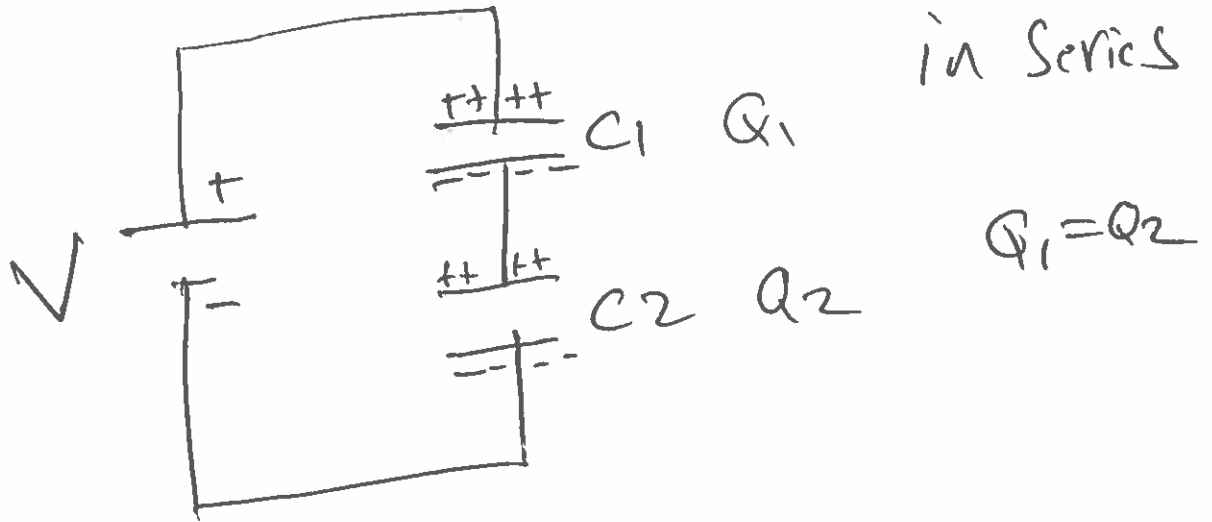
$$C_{\text{Tot}} V = C_1 V + C_2 V$$

$$C_{\text{Tot Parallel}} = C_1 + C_2$$

$$\text{If } C_1 = 5 \mu\text{F} \quad C_2 = 10 \mu\text{F}$$

$$C_{\text{Tot}} = C_1 + C_2 = 5 \mu\text{F} + 10 \mu\text{F}$$

$$C_{\text{Tot}} = 15 \mu\text{F}$$



$$V_1 = \frac{Q}{C_1} \quad V_2 = \frac{Q}{C_2}$$

$$V_{\text{Tot}} = V = V_1 + V_2$$

$$\frac{Q}{C_{\text{Tot}}} = \frac{Q}{C_1} + \frac{Q}{C_2}$$

$$\frac{1}{C_{\text{Tot}} \text{ Series}} = \frac{1}{C_1} + \frac{1}{C_2}$$

## Capacitors

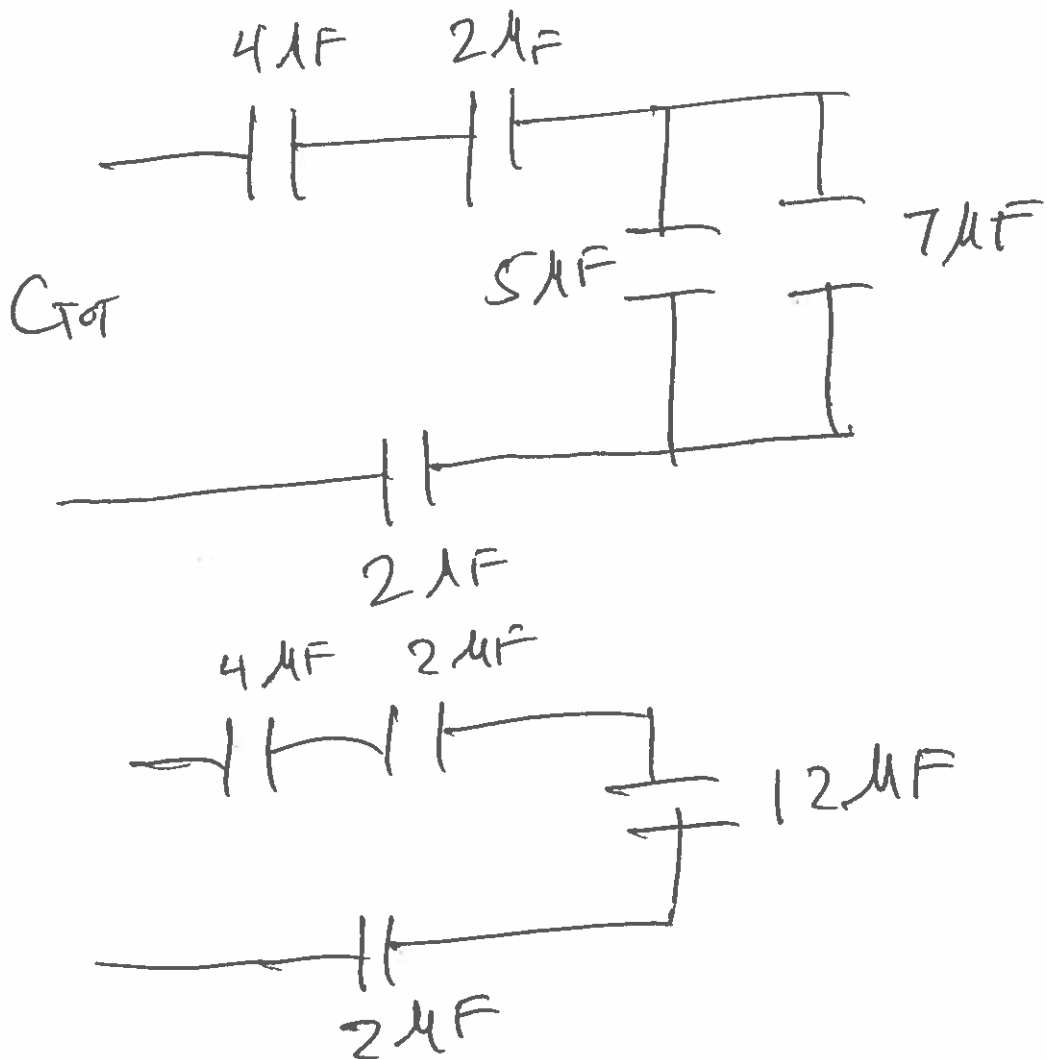
Series  $\frac{1}{C_{TOT}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_n}$

Parallel  $C_{TOT} = C_1 + C_2 + \dots + C_n$

## Resistors

Series  $R_{TOT} = R_1 + R_2 + \dots + R_n$

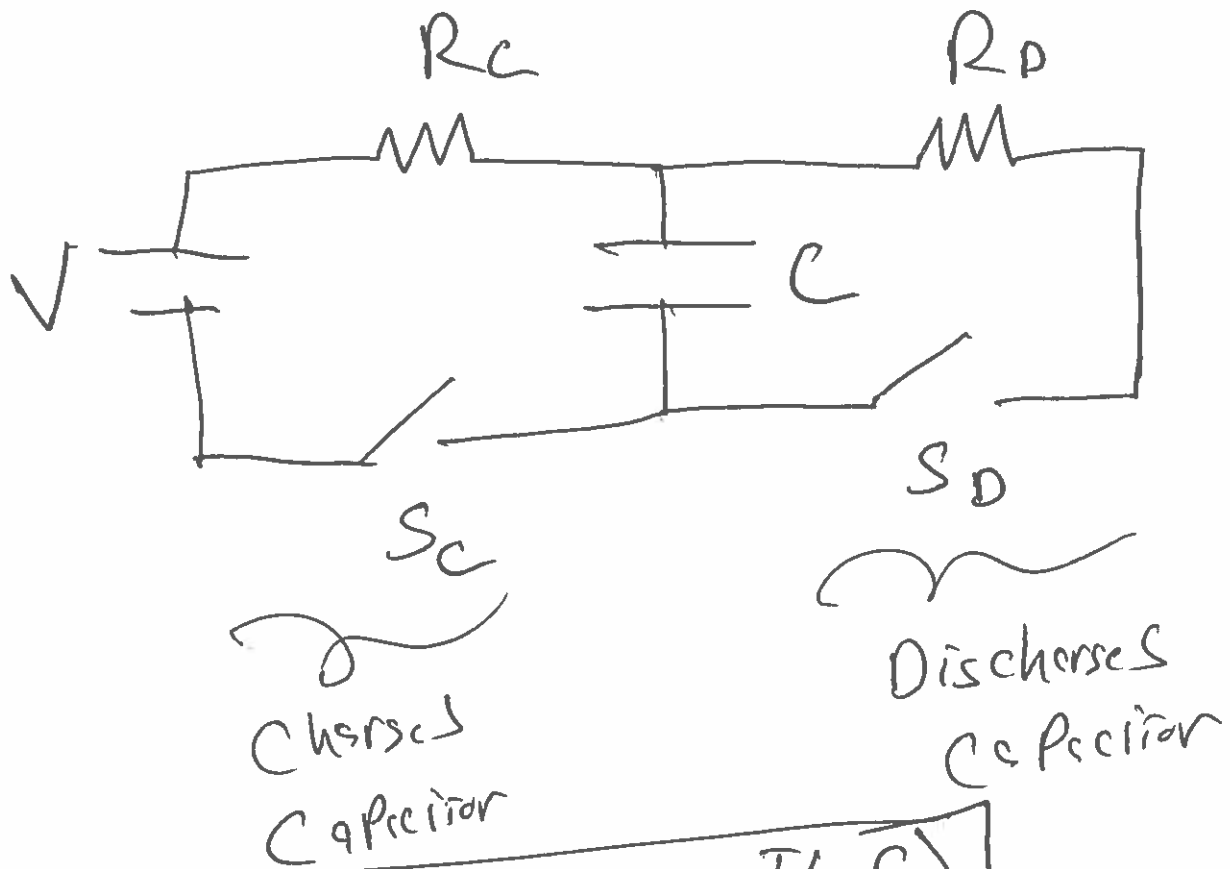
Parallel  $\frac{1}{R_{TOT}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$



$$\frac{1}{C_{\text{TOT}}} = \frac{1}{4\mu\text{F}} + \frac{1}{2\mu\text{F}} + \frac{1}{12\mu\text{F}} + \frac{1}{2\mu\text{F}}$$

$$\frac{1}{C_{\text{TOT}}} = \frac{3 + 6 + 1 + 6}{12\mu\text{F}} = \frac{16}{12\mu\text{F}}$$

$$C_{\text{TOT}} = \frac{12\mu\text{F}}{16} = \boxed{\frac{3}{4}\mu\text{F}}$$



Charging

$$Q(t) = Q_F (1 - e^{-t/R_C C})$$

$Q_F = CV$

$$e^{-1} = \sim 0,37 \Rightarrow T = R_C C = \tau$$

$\tau$  is capacitive time constant

$$\tau = RC = (1000 \Omega)(10,000 \mu F)$$

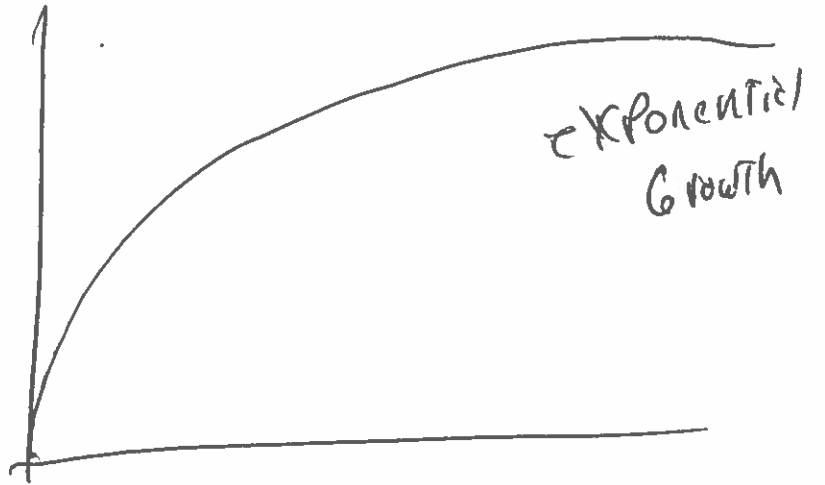
$$\tau = (10^3)(10^4 \times 10^{-6}) \Omega F$$

$$\tau = 10 S$$

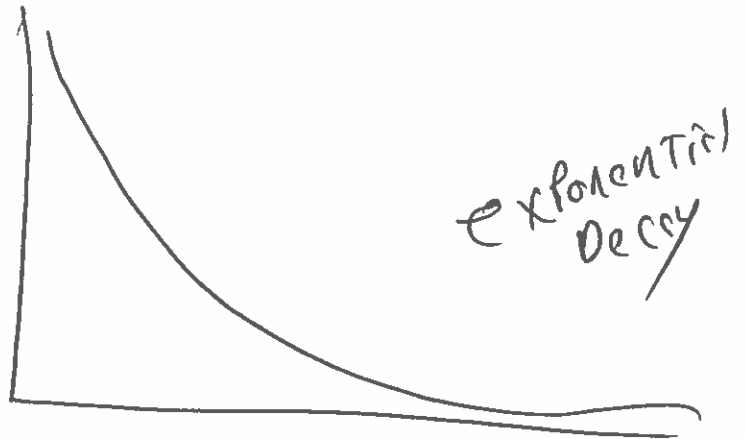


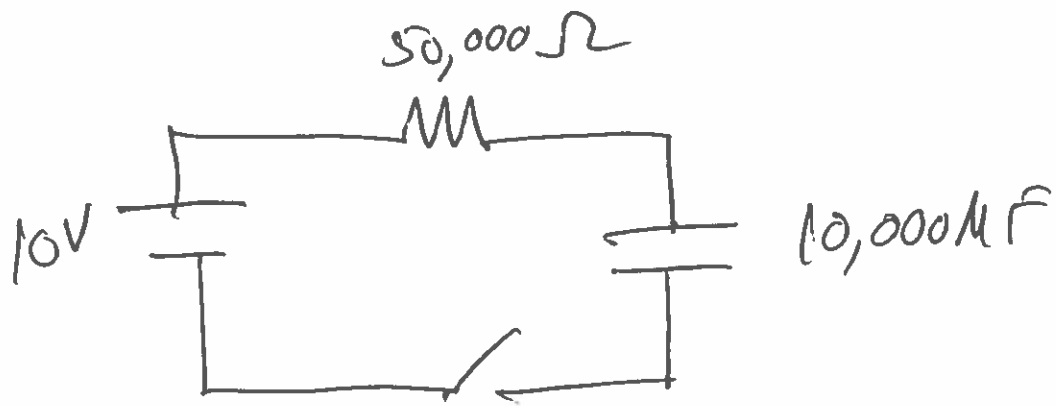
Discharging  $Q(t) = Q_f e^{-t/RC}$   $Q_f = CV$

Charging



Discharging





$Q = ?$  after  $t = 30s$ ?  
 $= 1000s$ ?

$$Q = Q_0 (1 - e^{-t/RC})$$

$$Q_0 = (10,000 \mu F)(10V)$$

$$= 100,000 \mu C$$

$$= 0.10 \text{ mC}$$

$$Q(t=30s) = (0.10 \text{ mC}) (1 - e^{-30s / (50,000 \Omega)(10,000 \times 10^{-6} \text{ F})})$$

$Q(t=30s) = 5.8 \text{ mC}$
$Q(t=1000s) = 86 \text{ mC}$