

Index of refraction

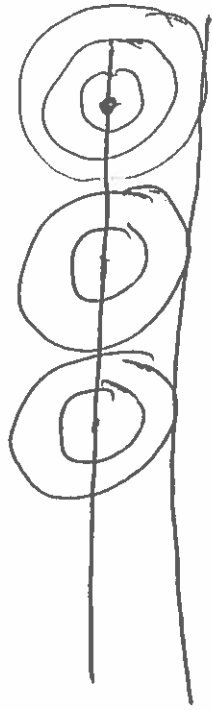
$$n = \frac{c}{v} = \frac{\text{Speed of light in vacuum}}{\text{Speed of light in medium}}$$

$$n > 1 \quad \text{Speed of light in vacuum} \geq \text{Speed of light in medium}$$

$$n_{\text{air}} = 1.00023$$

$$n_{\text{water}} = 1.333 \Rightarrow n_{\text{water}} \sim \frac{3}{4} c$$

$$n_{\text{diamond}} = 2.419 = n_{\text{diamond}} \sim \frac{1}{2} c$$

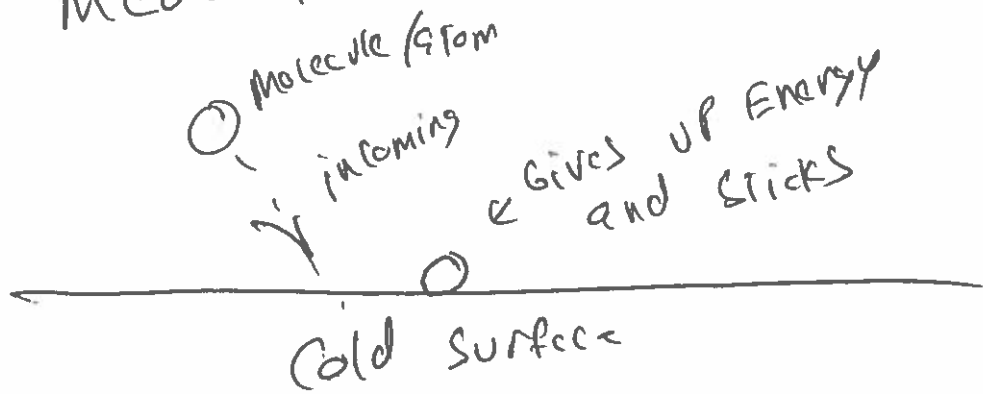


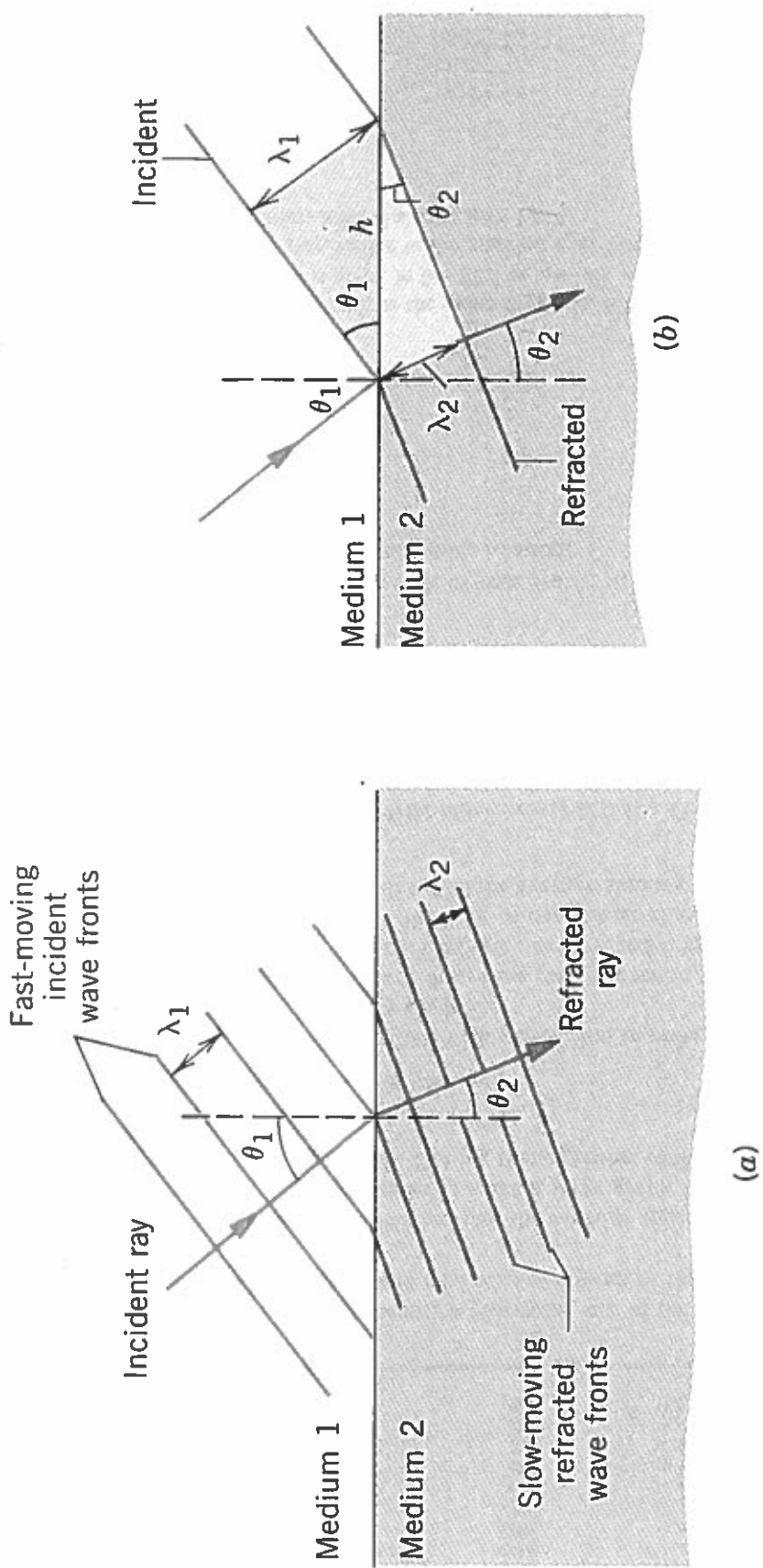
light slows down
in a medium because
it is momentarily absorbed
by atoms, molecules in medium.

If the energy is not
a value useable by the

absorber, the energy is
re-emitted at some energy
which means some frequency though
often shorter wave length.

Greater $n \Rightarrow$ more optically dense the
medium, the slower light travels.





$$n = \frac{c}{v} = \frac{\lambda_0 f_0}{\lambda_m f_m}$$

λ_0 - wavelength in vacuum

λ_m - wavelength in medium

If Energy stays same $E = hf$

$$f_0 = f_m$$

$$n = \frac{\lambda_0}{\lambda_m} \Rightarrow \lambda_m = \lambda_n = \frac{\lambda_0}{n}$$

$$\lambda_0 = 750 \text{ nm} \quad \lambda_{\text{water}}$$

Average Person Visible light 400nm \rightarrow 700nm
Violet Red

$$\lambda_w = \frac{\lambda_0}{n} = \frac{750 \text{ nm}}{1.33} = \text{~~562.6~~ 562.6 nm}$$

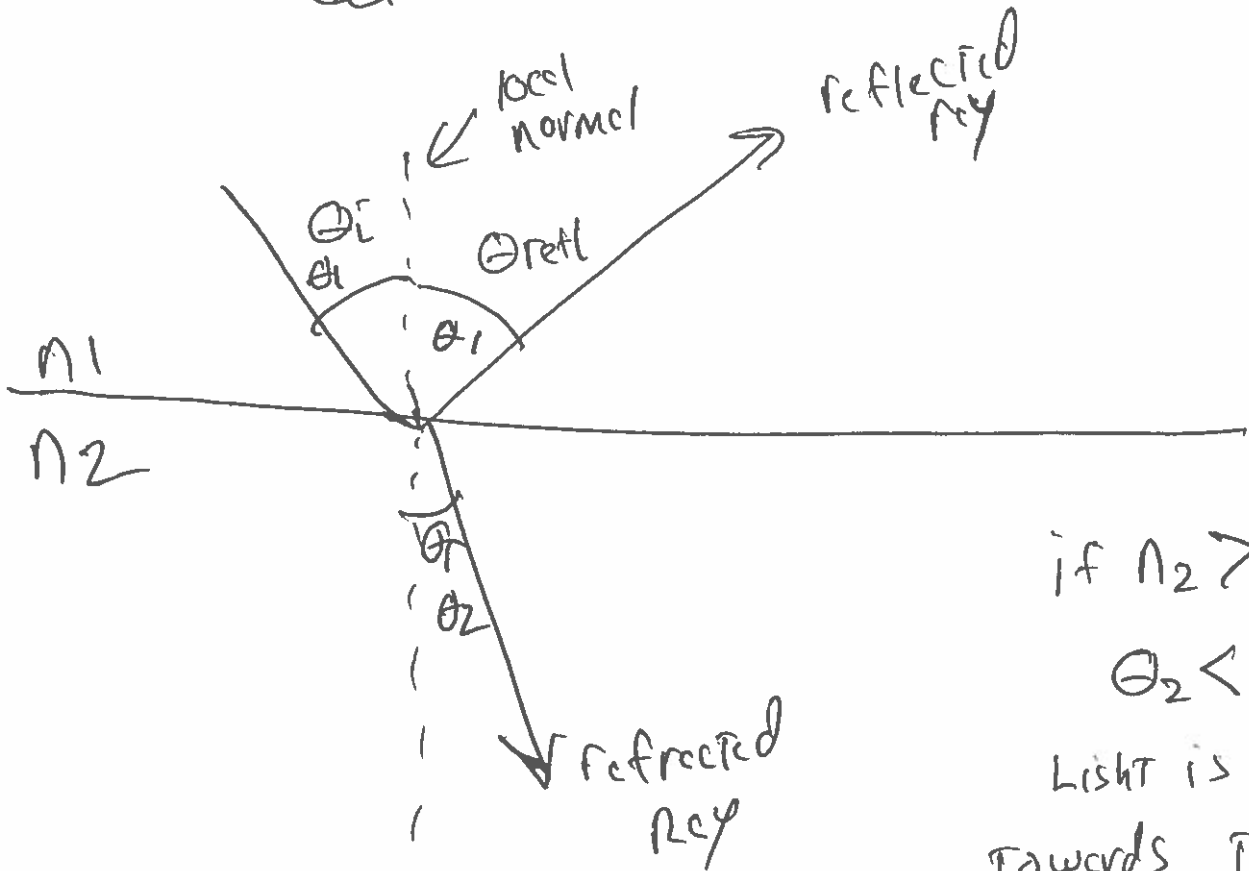
750 nm IR

562 nm \sim Greenish

$$\theta_r = \theta_i \quad \text{Law of reflection}$$

Snell's Law

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$



if $n_2 > n_1$

$$\theta_2 < \theta_1$$

Light is bent
towards the
normal

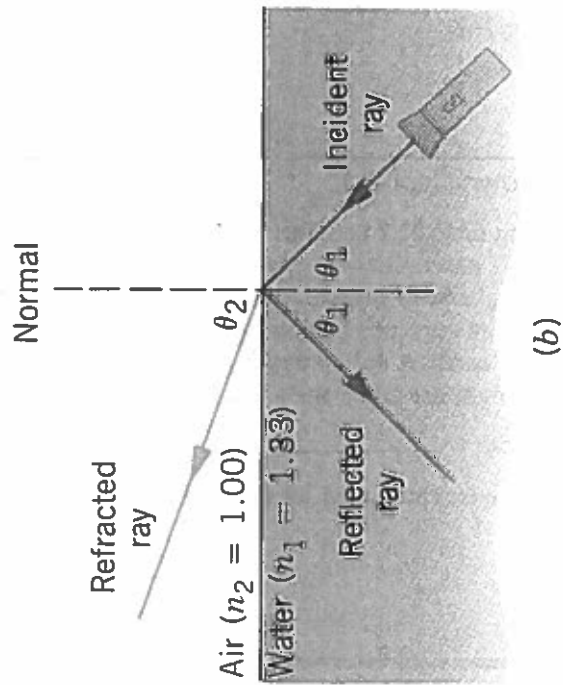
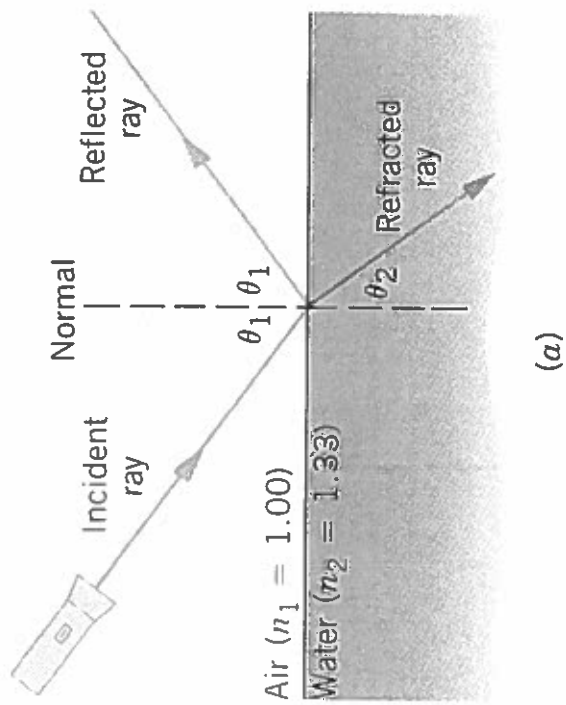


FIGURE 26.1 a, b 192

Light incident on a slab of glass

$$n_g = 1.50 \quad \theta_{\text{incidence}} = 45^\circ$$

$$\theta_{\text{reflection}} = ? \quad \theta_{\text{refraction}} = ?$$

$$\theta_{\text{refl}} = \theta_i = 45^\circ$$

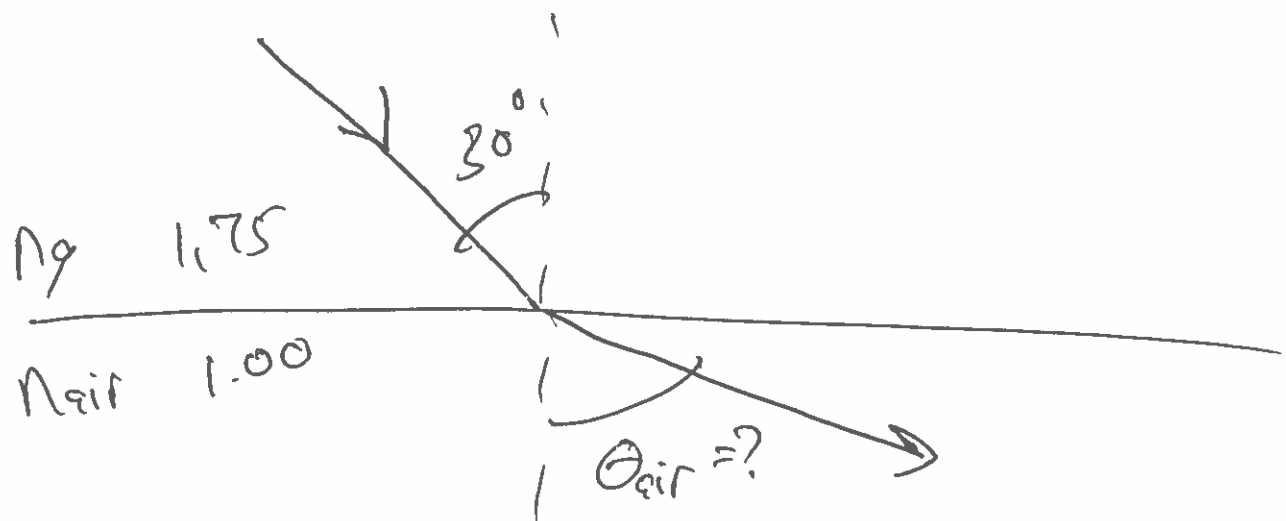
$$n_{\text{air}} \sin \theta_i = n_{\text{glass}} \sin \theta_{\text{refr}}$$

$$\sin \theta_{\text{refr}} = \sin \theta_i \left(\frac{n_{\text{air}}}{n_{\text{glass}}} \right)$$

$$\sin \theta_{\text{refr}} = \sin(45^\circ) \left(\frac{1}{1.5} \right) = 0.4714$$

$$\theta_{\text{refr}} = \sin^{-1}(0.4714) = 28.1^\circ$$

2nd light ray in a glass ($n_g = 1.75$)
 $\theta_i = 30^\circ$ $\theta_{air} = ?$



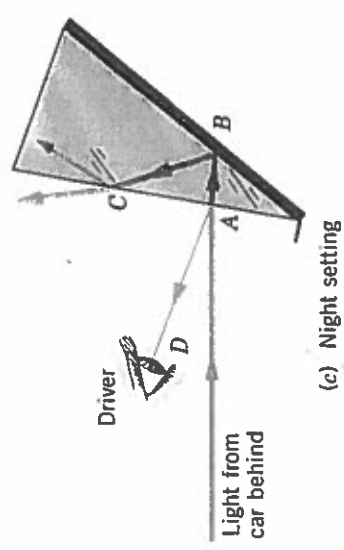
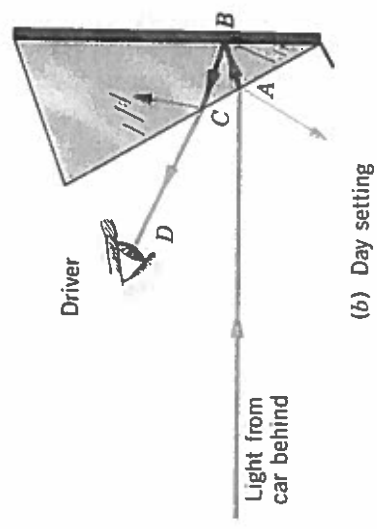
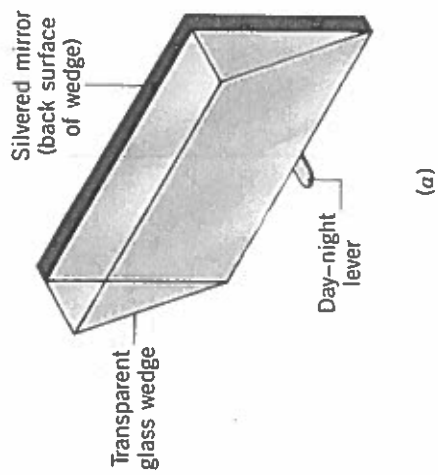
Snell's Law

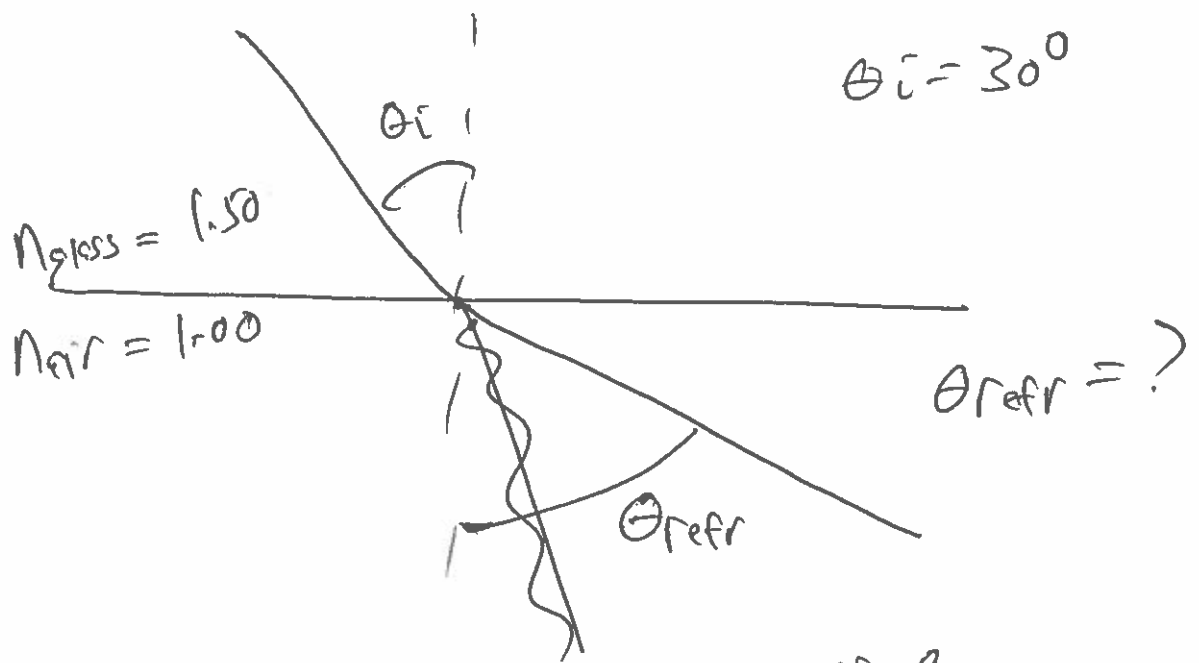
$$n_{air} \sin \theta_{air} = n_g \sin \theta_g$$

$$\sin \theta_{air} = \frac{n_g}{n_{air}} \sin \theta_g$$

$$\sin(\theta_{air}) = \left(\frac{1.75}{1.00} \right) \sin(30^\circ) = 0.875$$

$$\theta_{air} = \sin^{-1}(0.875) = \boxed{61.0^\circ}$$





$$n_{\text{air}} \sin \theta_{\text{refr}} = n_{\text{glass}} \sin \theta_{\text{glass}}$$

$$\sin \theta_{\text{refr}} = \frac{n_{\text{glass}}}{n_{\text{air}}} \sin \theta_{\text{glass}}$$

$$\sin \theta_{\text{refr}} = \frac{1.50}{1.00} \sin (30) = 0.75$$

$$\theta_{\text{refr}} = \sin^{-1}(0.75) = 48.6^\circ$$

Biggest angle of refraction = 90°

What angle of incidence
gives 90° ?

$$n_{\text{air}} \sin \theta_{\text{air}} = n_{\text{glass}} \sin \theta_{\text{glass}}$$

$$\sin \theta_{\text{glass}} = \frac{n_{\text{air}}}{n_{\text{glass}}} \sin \theta_{\text{air}}$$

$$\sin \theta_{\text{glass}} = \frac{1.00}{1.50} \sin(90^\circ)$$

$$\sin \theta_{\text{glass}} = \frac{1}{1.50}$$

$$\theta_{\text{glass}} = \sin^{-1}\left(\frac{1}{1.50}\right) = \underline{41.8^\circ}$$

$$\theta_{\text{glass}} = 41.8^\circ \Rightarrow \theta_{\text{critical angle}}$$

