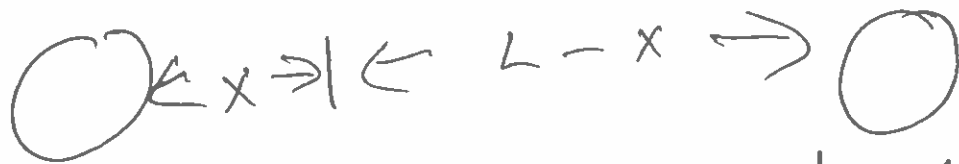


$$f = 200 \text{ Hz} \Rightarrow \lambda = \frac{340 \text{ m/s}}{200 \text{ Hz}} = 1.70 \text{ m}$$

AT center Both speaker sounds travel same distance \Rightarrow constructive interference

$$L = 10 \text{ m}$$



Points x where sounds cancel.

$$\text{Path difference} = (m + \frac{1}{2}) \lambda$$

for
Destructive
interference

$$m = 0, 1, 2, \dots$$

$$\text{Path difference} = \left| \left(\frac{L}{2} - x \right) - x \right|$$

$$\left| L - 2x \right| = (m + \frac{1}{2}) \lambda$$

destructive
interference
or sounds
cancel.

$$L - 2x = (m + \frac{1}{2})\lambda$$

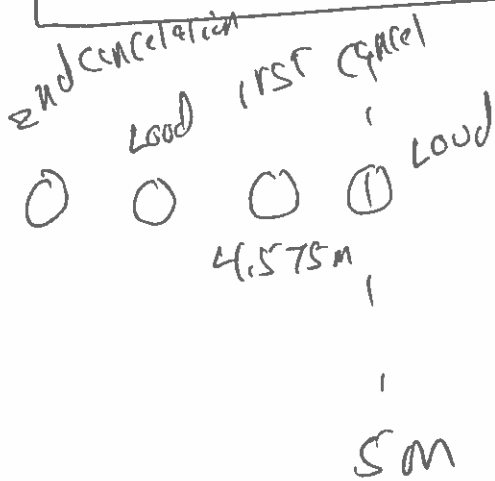
$$2x = L - (m + \frac{1}{2})\lambda$$

$$x = \frac{1}{2}L - \frac{1}{2}(m + \frac{1}{2})\lambda$$

$$m = 0$$

$$x_0 = \frac{1}{2}(10\text{m}) - \frac{1}{2}(\frac{1}{2})(1.7\text{m})$$

$$x_0 = 4.575\text{m}$$



$$x = \frac{1}{2}L - \frac{1}{2}(m + \frac{1}{2})\lambda$$

$$x = \frac{1}{2}L - \frac{1}{2}m\lambda$$

Cancel condition
Load condition

$$X_1 = \frac{1}{2} (10\text{m}) - \frac{1}{2} \left(1 + \frac{1}{2}\right) (1.7\text{m})$$

$$X_1 = 3.725\text{m}$$

~~$$X = \frac{1}{2} L - \frac{1}{2} \left(m + \frac{1}{2}\right) \lambda \leq 5\text{m}$$~~

~~$$\frac{1}{2} (10\text{m}) - \frac{1}{2} \left(m + \frac{1}{2}\right) (1.7\text{m}) \leq 5\text{m}$$~~

~~$$m + \frac{1}{2} \leq \frac{2}{1.7}$$~~

$$X_2 = 2.875\text{m}$$

$$X_3 = 2.025\text{m}$$

$$X_4 = 1.175\text{m}$$

$$X_5 = 0.325\text{m}$$

$$X_6 = -0.525\text{m} \quad \text{cannot be}$$

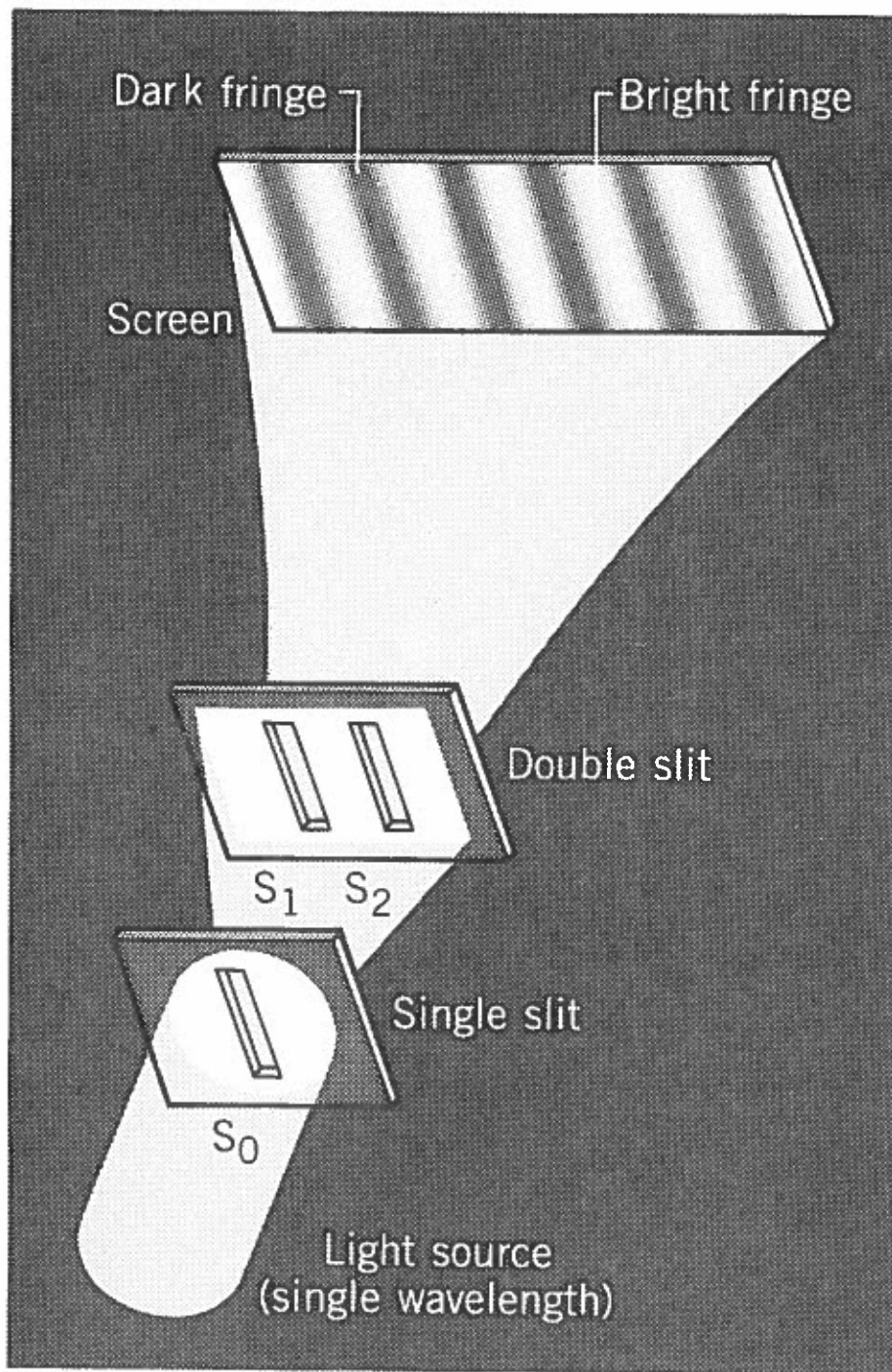
$$\text{Phase diff} = \left(\text{Path diff} \right) = m \lambda \Rightarrow \text{constructive}$$

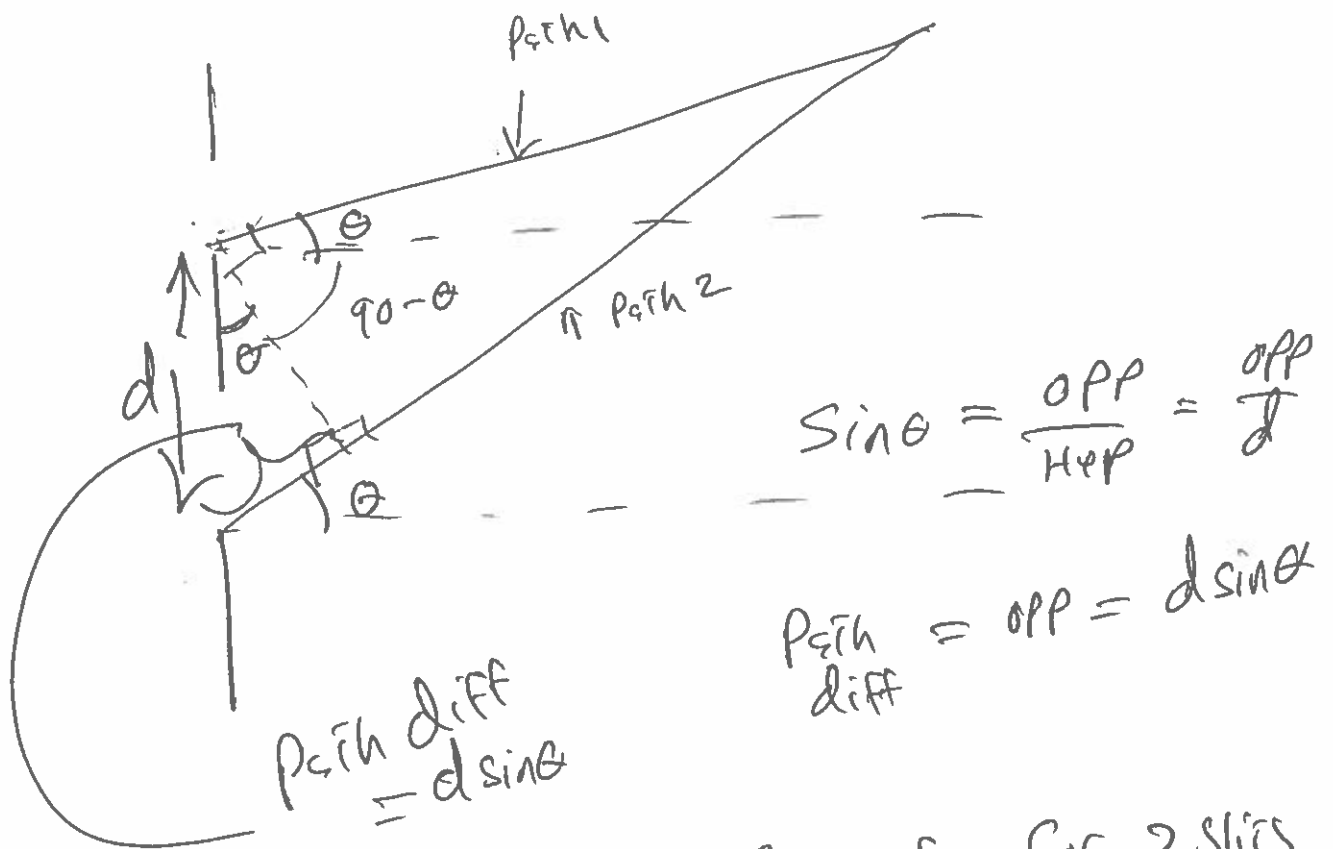
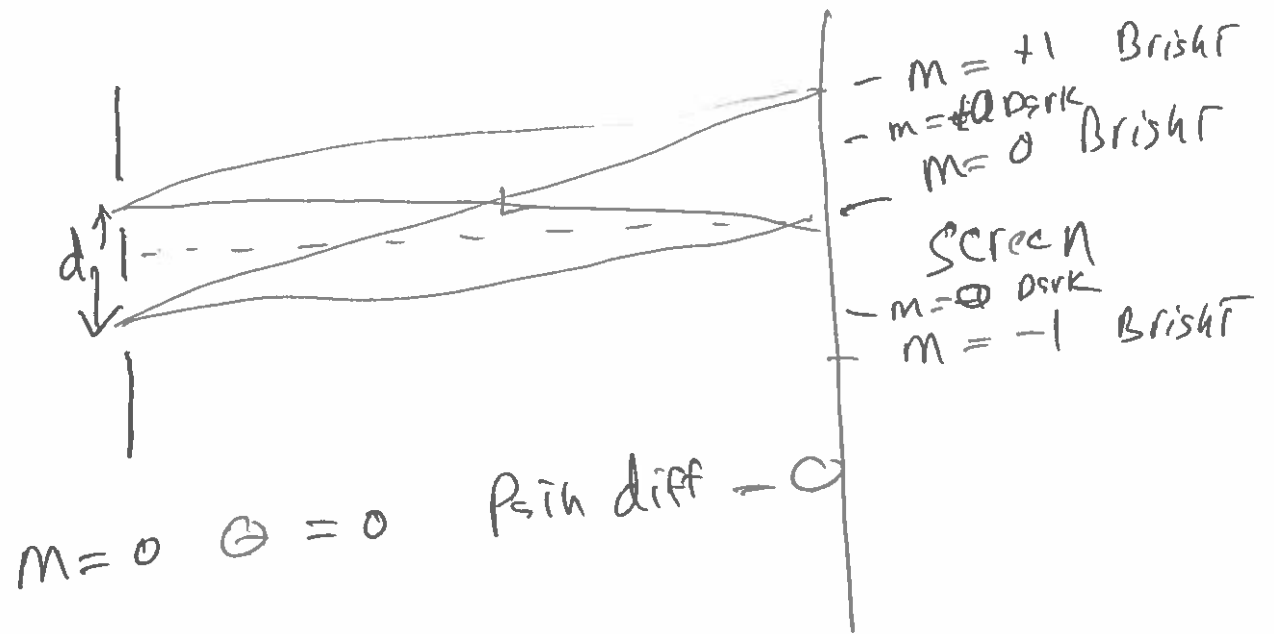
$$\text{Phase diff} = \left| \text{Path diff} \right| = \left(m + \frac{1}{2} \right) \lambda \Rightarrow \text{destructive}$$

m is integers

usually $0, 1, 2, 3, \dots$

○ occasionally 0 is not allowed.





Conditions for fringes for 2 slits

bright $\Rightarrow d \sin \theta = m \lambda$

dark $\Rightarrow d \sin \theta = (m + \frac{1}{2}) \lambda$

Path diff

ex/ $d = 5.6 \times 10^{-6} \text{ m}$ $\lambda = 546 \text{ nm}$
 θ 's of First 3 bright fringes

For bright $d \sin \theta = m \lambda$

$$\sin \theta = \frac{m \lambda}{d}$$

$$\sin \theta_1 = \frac{\lambda}{d} = \frac{546 \times 10^{-9} \text{ m}}{5.6 \times 10^{-6} \text{ m}} \Rightarrow \theta_1 = 5.6^\circ$$

$$\sin \theta_2 = \frac{2\lambda}{d} = \frac{2(546 \times 10^{-9} \text{ m})}{5.6 \times 10^{-6} \text{ m}} \Rightarrow \theta_2 = 11.2^\circ$$

$$\sin \theta_3 = \frac{3\lambda}{d} = \frac{3(546 \times 10^{-9} \text{ m})}{5.6 \times 10^{-6} \text{ m}} \Rightarrow \theta_3 = 17.0^\circ$$

How many bright fringes?

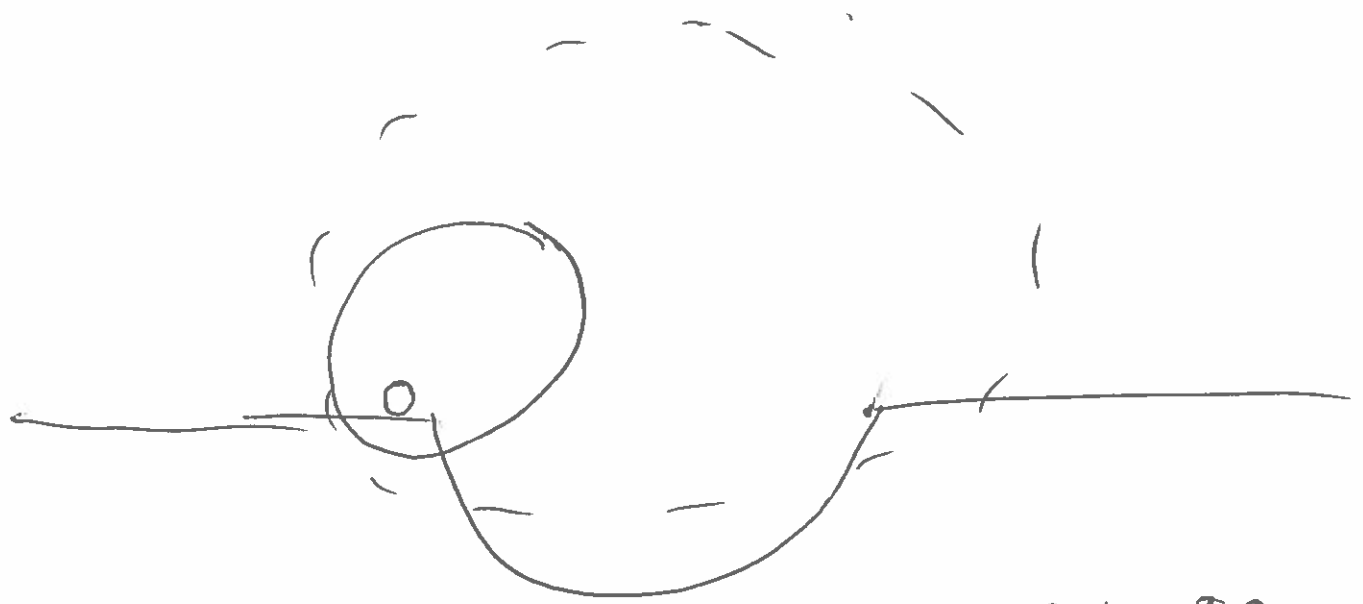
Largest $\theta \rightarrow 90^\circ$

$$m\lambda = d \sin \theta \Rightarrow m = \frac{d \sin \theta}{\lambda}$$

$$m = \frac{d \sin 90}{\lambda} = \frac{d}{\lambda} = \frac{5.6 \times 10^{-6} \text{ m}}{546 \times 10^{-9} \text{ m}}$$

$$m = 10.2 \Rightarrow m \leq 10$$

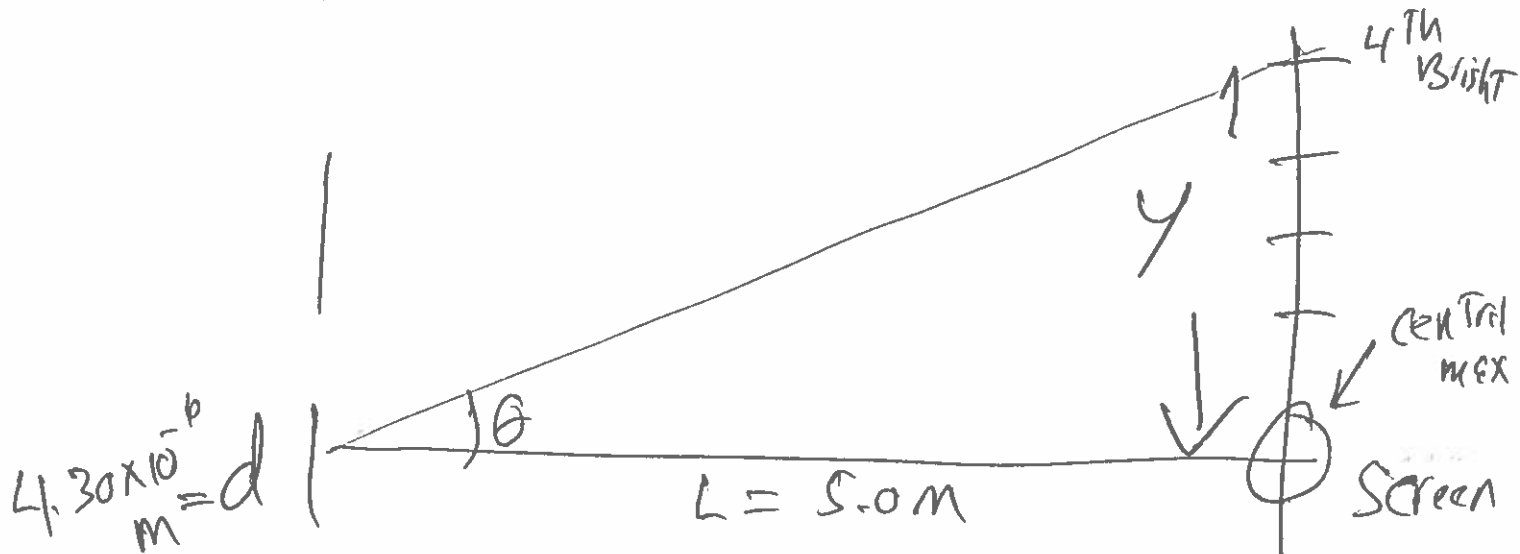
So total fringes = $2(10) + 1 = 21$



Noticing disruptions require probes to be about same size.

↳ - Visible light are $400 \text{ nm} - 700 \text{ nm}$
 $4.0 \times 10^{-7} \text{ m} - 7.0 \times 10^{-7} \text{ m}$
Slit widths $\sim 10^{-7} \text{ m}$ ($10^{-5} - 10^{-8}$)

ex/ Two slits separated by $4.30 \times 10^{-6} \text{ m}$
 Red light $\lambda = 690 \text{ nm}$ Screen 5.0 m
 away how far is 4th bright fringe
 from center maximum



2 slits $d \sin \theta = m \lambda$

$$\sin \theta = \frac{m \lambda}{d}$$

$$\theta = \sin^{-1} \left(\frac{4}{4.30 \times 10^{-6} \text{ m}} \right) (690 \times 10^{-9} \text{ m})$$

$$\tan \theta = \frac{y}{L} \Rightarrow y = L \tan \theta$$

$$y = 5.00 \text{ m} \tan \left(\sin^{-1} \left(\frac{4}{4.30 \times 10^{-6} \text{ m}} \right) (690 \times 10^{-9} \text{ m}) \right)$$

$$y = 4.19 \text{ m}$$

$$d = 7.3 \times 10^{-6} \text{ m} \quad \lambda = 480 \text{ nm}$$

Q: What angle is 2nd dark fringe?

dark fringes

$$d \sin \theta = (m + \frac{1}{2}) \lambda$$

$$\sin \theta = \frac{(m + \frac{1}{2}) \lambda}{d}$$

1st dark fringe $m = 0$

2nd dark fringe $m = 1$

dark $m = -1$ bright $m = -1$ dark $m = 0$ central bright $m = 0$ dark $m = 0$ bright $m = 1$ dark $m = 1$

$$\sin \theta = \frac{(1 + \frac{1}{2})(480 \times 10^{-9} \text{ m})}{7.3 \times 10^{-6} \text{ m}} = \frac{3}{2} \frac{(480 \times 10^{-9})}{(7.3 \times 10^{-6})}$$

$$\sin \theta = 10986 \quad \theta = \sin^{-1}(10986)$$

$$\theta = 5.6^\circ$$